

1. Log in
2. Unit 4

- Writing Methods
- **Recursion - MORE**
- Classes and Objects

Oct 16-7:52 AM

Analyze this user-defined method:

addEm(4) = ?

Answer: [REDACTED]

```
public static int addEm(int n)
{
    if(n==0)
        return 15;
    else
        return n + addEm(n-1);
}
```

Nov 5-8:02 AM

Step-by-Step Analysis ...

```
public static int minus(int n)
{
    if(n==1)
        return 1;
    else
        return n - minus(n-1);
}
```

minus(4) = ?

Nov 5-12:51 PM

Step-by-Step Analysis ...

```
public static int minus(int n)
{
    if(n==1)
        return 1;
    else
        return n - minus(n-1);
}
```

$$\text{minus}(4) = 4 - \text{minus}(3)$$

$\downarrow$
 $3 - \text{minus}(2)$

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Step-by-Step Analysis ...

```
public static int minus(int n)
{
    if(n==1)
        return 1;
    else
        return n - minus(n-1);
}
```

```
minus(4) = 4 - minus(3)
           ↓
           3 - minus(2)
               ↓
               2 - minus(1)
```

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Step-by-Step Analysis ...

```
public static int minus(int n)
{
    if(n==1)
        return 1;
    else
        return n - minus(n-1);
}
```

```

minus(4) = 4 - minus(3)
           ↓
           3 - minus(2)
               ↓
               2 - minus(1)
                   ↓
                   1

```

Now the computer works backward (note: answer = 2)

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Here's a tricky one ...

```
public static void divide(int n){
    if(n<=1)
        System.out.print(n);
    else{
        divide(n/2);
        System.out.print(", "+n);
    }
}
```

divide(9) =

Nov 5-12:56 PM

Here's a tricky one ...

```
public static void divide(int n){
    if(n<=1)
        System.out.print(n);
    else{
        divide(n/2);
        System.out.print(", "+n);
    }
}
```

divide(9) = divide(4) and then print " ,9" //n=9

Nov 5-12:56 PM

Here's a tricky one ...

```
public static void divide(int n){
    if(n<=1)
        System.out.print(n);
    else{
        divide(n/2);
        System.out.print(", "+n);
    }
}
```

divide(9) = divide(4) and then print " ,9" //n=9

↓

divide(2) and then print " , 4" //n=4

Nov 5-12:56 PM

Here's a tricky one ...

```
public static void divide(int n){
    if(n<=1)
        System.out.print(n);
    else{
        divide(n/2);
        System.out.print(", "+n);
    }
}
```

divide(9) = divide(4) and then print " ,9" //n=9

↓

divide(2) and then print " , 4" //n=4

↓

divide(1) and then print " , 2" //n=2

Nov 5-12:56 PM

Here's a tricky one ...

```
public static void divide(int n){
    if(n<=1)
        System.out.print(n);
    else{
        divide(n/2);
        System.out.print(", "+n);
    }
}
```

divide(9) = divide(4) and then print " ,9" //n=9

↓

divide(2) and then print " , 4" //n=4

↓

divide(1) and then print " , 2" //n=2

↓

print "1" //n=1

Remember, JAVA
now compiles this
"bottom-up"

Nov 5-12:56 PM

Here's how the divide() method gets compiled ...

Remember, JAVA
now compiles this
"bottom-up"

OUTPUT

divide(9) = divide(4) and then print " ,9"

↓

divide(2) and then print " , 4"

↓

divide(1) and then print " , 2"

↑

print "1"

1

Nov 5-12:56 PM

Here's how the divide() method gets compiled ...

Remember, JAVA
now compiles this
"bottom-up"divide(9) = divide(4) and then print " ,9"↓
divide(2) and then print " ,4"↑
1 and then print " ,2"

OUTPUT

1,2

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Here's how the divide() method gets compiled ...

Remember, JAVA
now compiles this
"bottom-up"divide(9) = divide(4) and then print " ,9"↑
1,2 and then print " ,4"

OUTPUT

1,2,4

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Here's how the divide() method gets compiled ...

Remember, JAVA
now compiles this
"bottom-up"divide(9) = 1,2,4 and then print " ,9"

OUTPUT

1,2,4,9

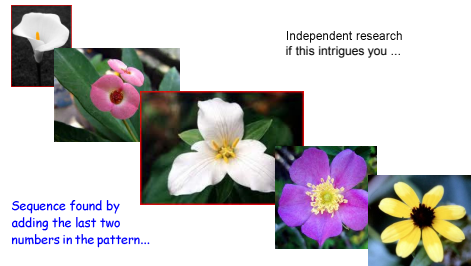
Final Output for divide(9) = 1,2,4,9

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Mathematics, The World Around Us, and Nature ...

Fibonacci: 1, 1, 2, 3, 5, 8, 13, 21, 34, ...

Golden Ratio ...

 $3/2 = 1.5$ $5/3 = 1.67$ $8/5 = 1.6$ $13/8 = 1.625$ $21/13 = 1.61538$ 

Nov 5-1:42 PM

Fibonacci: 1, 1, 2, 3, 5, 8, 13, 21, ...

I want to calculate
the 4th number ...

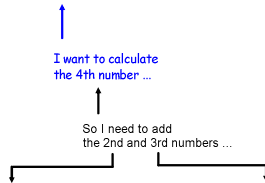
Nov 5-1:47 PM

Fibonacci: 1, 1, 2, 3, 5, 8, 13, 21, ...

I want to calculate
the 4th number ...So I need to add
the 2nd and 3rd numbers ...

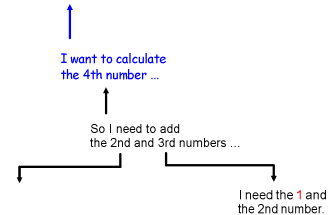
Nov 5-1:47 PM

Fibonacci: 1, 1, 2, 3, 5, 8, 13, 21, ...



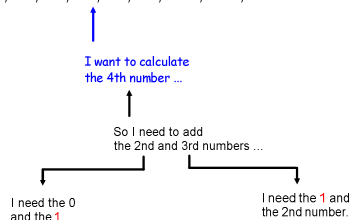
Nov 5-1:47 PM

Fibonacci: 1, 1, 2, 3, 5, 8, 13, 21, ...



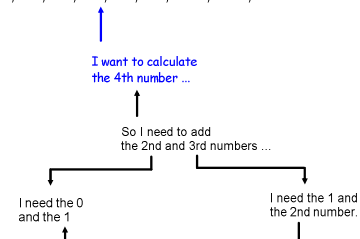
Nov 5-1:47 PM

Fibonacci: 1, 1, 2, 3, 5, 8, 13, 21, ...



Nov 5-1:47 PM

Fibonacci: 1, 1, 2, 3, 5, 8, 13, 21, ...



Nov 5-1:47 PM

Here's a user-defined fibonacci method() ...

```
public static int fib(int n){
    if(n==0){
        return 0;
    }
    else if(n==1){
        return 1;
    }
    else{
        return fib(n-1)+fib(n-2);
    }
}
```

$\text{fib}(4) = \text{fib}(3) + \text{fib}(2)$

Nov 5-1:53 PM

Here's a user-defined fibonacci method() ...

```
public static int fib(int n){
    if(n==0){
        return 0;
    }
    else if(n==1){
        return 1;
    }
    else{
        return fib(n-1)+fib(n-2);
    }
}
```

$\text{fib}(4) = \text{fib}(3) + \text{fib}(2)$
 $\text{fib}(2) = \text{fib}(1) + \text{fib}(0)$

Nov 5-1:53 PM

Here's a user-defined fibonacci method() ...

```
public static int fib(int n){
    if(n==0){
        return 0;
    }
    else if(n==1){
        return 1;
    }
    else{
        return fib(n-1)+fib(n-2);
    }
}
```

fib(4) = fib(3) + fib(2)
fib(2) + fib(1) fib(1) + fib(0)

Nov 5-1:53 PM

Here's a user-defined fibonacci method() ...

```
public static int fib(int n){
    if(n==0){
        return 0;
    }
    else if(n==1){
        return 1;
    }
    else{
        return fib(n-1)+fib(n-2);
    }
}
```

fib(4) = fib(3) + fib(2)
fib(2) + fib(1) fib(1) + fib(0)
 1 0

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Here's a user-defined fibonacci method() ...

```
public static int fib(int n){
    if(n==0){
        return 0;
    }
    else if(n==1){
        return 1;
    }
    else{
        return fib(n-1)+fib(n-2);
    }
}
```

fib(4) = fib(3) + fib(2)
fib(2) + fib(1) fib(1) + fib(0)
fib(1) + fib(0) 1 1 0

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To solve, remember JAVA compiles bottom-up ...

fib(4) = fib(3) + fib(2)
fib(2) + fib(1) fib(1) + fib(0)
fib(1) + fib(0) 1 1 0
1 0 1 0

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To solve, remember JAVA compiles bottom-up ...

fib(4) = fib(3) + fib(2)
fib(2) + 1 1 + 0
1 + 0 1 0

Nov 5-1:53 PM

To solve, remember JAVA compiles bottom-up ...

fib(4) = fib(3) + 1
1 + 1

Nov 5-1:53 PM

To solve, remember JAVA compiles bottom-up ...

$\text{fib}(4) = 2 + 1$

So, then $\text{fib}(4) = 3$

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Example of recursion that doesn't work ...

Hope you have a computer with infinite memory space!

```
package unit04;

public class infiniteRecursion {
    public static int goodLuck(int a)
    {
        if(a==5)
            return a;
        else
            return a+goodLuck(a+1);
    }
    public static void main(String[] args) {
        System.out.println(goodLuck(3)); //easy, this is 12
        System.out.println(goodLuck(7)); //good luck! Infinite Math
    }
}
```

Nov 6-8:00 AM

```
package unit04;
public class voidReturnExample {
    public static void nothing(int z, int m)
    {
        if(z<m) {
            for(int i=0; i<z; i++)
                System.out.print("XO");
            System.out.println("");
            nothing(z+1,m);
        }
        else if (z==m) {
            for(int i=0; i<z; i++)
                System.out.print("-");
            System.out.println("");
            nothing(z+1,m);
        }
        else
            System.out.print("Process Complete"); //This is base case - no return
    }
    public static void main(String[] args) {
        returnNothing(7,10);
    }
}
```

Example of a
user-defined
method that
doesn't return
anything ...

//Notice, we aren't having
//anything returned to the
//main method. We are simply
//having it follow directions.

Nov 6-8:00 AM

Things to do ...

1. Unit 4 WS 01 should be done.
2. Wrap up Unit 4 WS 02 Introduction to Recursion
3. Work on Unit 4 WS 03 More Recursion

Oct 16-9:12 AM